

7.41) $X = \text{time to position}$ $\mu_x = 11, \sigma_x = 2, \sigma^2_x = 4$
 $Y = \text{time to attach}$ $\mu_y = 20, \sigma_y = 4, \sigma^2_y = 16$

a) TOTAL meantime = $\mu_x + \mu_y = 11 + 20 = \boxed{31 \text{ sec}}$

b) NO. the meantime would not be changed by the change in variability.

c) $\sigma^2_{x+y} = \sigma^2_x + \sigma^2_y = 4 + 16 = 20$
 $\sigma_{x+y} = \sqrt{20} = \boxed{4.4721 \text{ sec}}$

7.42) a) 100-ohm $\rightarrow N(100, 2.5) \leftarrow R_1$ $T = R_1 + R_2$
 250-ohm $\rightarrow N(250, 2.8) \leftarrow R_2$ $\mu_T = 100 + 250 = 350 \text{ ohms}$
 $\sigma_T = \sqrt{(2.5)^2 + (2.8)^2}$

$\boxed{N(350, 3.753)}$

$\sigma_T = 3.753 \text{ ohms}$

b) $P(345 < T < 355) = P\left(\frac{345-350}{3.753} < \frac{T-350}{3.753} < \frac{355-350}{3.753}\right)$

$= P(-1.33 < Z < 1.33)$

$= 0.8172$

$\sim 81.72\%$

The prob. that the total resistance is between 345 & 355 ohms is $\boxed{0.8172}$

7.43a) $\mu_x = 1.7176 \text{ toys}$
 $\sigma_x = 1.3106 \text{ toys}$

7.44) a) GAIN 30% \cap GAIN 30% = $1000(1.3)(1.3) = 1690$

$G \cap L = 1000(1.3)(.75) = 975$

or $L \cap G =$

$L \cap L = 1000(.75)(.75) = 562.5$

$P(G \cap G) = 0.25$

$P(G \cap L \text{ or } L \cap G) = 0.5$

$P(L \cap L) = 0.25$

• $X = \text{worth of stock}$

$$P(X > 1000) \rightarrow P(X = 1690) = \boxed{0.25}$$

b) $\mu_x = (1690)(0.25) + (975)(.5) + (5625)(0.25)$

$$\mu_x = \boxed{\$1050.63}$$

7.45) $F = \text{SSHA scores for female st. } \mu_F = 120, \sigma_F = 28, \sigma^2_F = 784$
 $M = \text{SSHA scores for male st. } \mu_m = 105, \sigma_m = 35, \sigma^2_m = 1225$

a) Randomly selected students would be unrelated.

b) $\mu_{F-m} = \mu_F - \mu_m = 120 - 105 = 15 \text{ points}$

$$\sigma_{F-m} = \sqrt{(28)^2 + (35)^2} = 44.8219 \text{ points}$$

c) No... we don't know if scores are normally distributed.

7.47) a) $\mu_x = \boxed{550^\circ\text{C}}$

$$\sigma_x = \boxed{5.7009^\circ\text{C}}$$

b) $\mu_{x-550} = \mu_x - 550 = 0^\circ\text{C}$

$$\sigma_{x-550} = 5.7009^\circ\text{C} \leftarrow \text{wouldn't change}$$

c) $Y = \frac{9}{5}X + 32$ $\mu_{\frac{9}{5}X+32} = \frac{9}{5}\mu_x + 32$

$$= \boxed{1022^\circ\text{F}}$$

$$\sigma_{\frac{9}{5}X+32} = \sqrt{\left(\frac{9}{5}\right)^2 \sigma_x^2} = \frac{9}{5}\sigma_x = \frac{9}{5}(5.7009) = \boxed{10.26^\circ\text{F}}$$

- 7.49) a) yes $\mu_{x+y} = \mu_x + \mu_y$
 b) NOT UNLESS WE KNOW X & Y ARE INDEPENDENT!

7.50) T = TORQUE, S = capping strength
 $N(7, 0.9)$ $N(10, 1.2)$

a) Yes, they are sep. machines

b) $P(T > S) = P(T - S > 0) = P\left(\frac{(T-S)+3}{1.5} > \frac{0+3}{1.5}\right)$

$T-S$ is $N(-3, 1.5)$
 $\mu_{T-S} = 7-10 = -3$
 $\sigma_{T-S} = \sqrt{(0.9)^2 + (1.2)^2} = 1.5$

$= P(Z > 2)$

$= 0.0228$

The prob. that the cap breaks is $\sim 2.28\%$

7.51) a) $\sigma^2_y = 0.41$ trucks
 $\sigma_y = 0.6403$ trucks

b) $\sigma^2_{x+y} = 0.89 + 0.41 = 1.3$

$\sigma_{x+y} = \sqrt{1.3} = 1.1402$ total vehicles

c) $\sigma^2_{350X+400Y} = 350^2 \sigma^2_x + 400^2 \sigma^2_y$
 $= 350^2 (.89) + 400^2 (.41)$
 $= 174,625$

$\sigma = \sqrt{174,625} = \417.88

7.52) L = Leona's score $N(24, 2)$
 F = Fred's score $N(24, 2)$

$P(|L-F| > 5) = P\left(\frac{|L-F-0|}{2.8284} \geq \frac{5-0}{2.8284}\right)$

$N(0, 2.8284)$ ~~$N(0, 1.7678)$~~
 $= P(|Z| > 1.7678)$
 $= 0.0771$

The prob. the scores differ by 5 or more points is 7.71%